

Tutorial - 1

Date _____

$$\begin{aligned} \text{Q1) (a) } \tau_{\text{obs}} &= \gamma \tau \\ &= \frac{\tau}{\sqrt{1 - \frac{v^2}{c^2}}} = 7.046 \times 10^{-6} \text{ s} \end{aligned}$$

$$\text{(b) } s = vt \Rightarrow 3000 = 3 \times 10^8 t \Rightarrow t = 10^{-5} \text{ s}$$

$$\begin{aligned} N &= N_0 e^{-t/\tau_{\text{obs}}} = 5000 \exp\left(-\frac{10^{-5}}{7.046 \times 10^{-6}}\right) \\ &= 12094.8 \end{aligned}$$

$$\therefore \# \text{ of particles} = 12100$$

$$\text{Q2) } \frac{mv^2}{r} = \frac{GMm}{r^2} \quad (\text{Since centripetal force} = \text{Gravitational Force})$$

$$\therefore v^2 = \frac{GM}{r}$$

$$\begin{aligned} M &= 6 \times 10^{24} \text{ kg} ; G = 6.67 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2} \\ r &= (160000 + 6.4 \times 10^6) \text{ m} \end{aligned}$$

$$v = 7810.64 \text{ m/s}$$

$$\gamma \Delta t_{\text{astronaut}} = \Delta t_{\text{earth}} \quad \text{--- (1)}$$

$$T = \Delta t_{\text{earth}} - \Delta t_{\text{astronaut}} = (\gamma - 1) \Delta t_{\text{astronaut}} \quad \text{--- (2)}$$

$$\Delta t_{\text{astronaut}} = \frac{2\pi r \times 22}{v} = 116096.6711 \text{ s}$$

$$\therefore T = (\gamma - 1)(116096.6711) = 39.3 \mu\text{s}$$

Q3) (a) NO
(b) YES

$$\begin{aligned} \text{(Q4)} \quad \Delta t_{\text{ast}} &= \frac{1}{\gamma} \Delta t_{\text{earth}} \\ &= \left(\sqrt{1 - (0.95)^2} \right) \times 80 \\ &= 24.98 \text{ years} \\ &\approx 25 \text{ years.} \end{aligned}$$